



Toward force detection of a cable-driven micromanipulator for a surgical robot based on disturbance observer

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Abstract. Force sensing plays an important role in minimally invasive surgery (MIS). Force sensing makes it possible for the surgeon to feel the tissue properties and apply an appropriate level force and avoid tissue damage. The micromanipulators are compact and to allow appropriate disinfection, it is inappropriate to integrate sensors at the end of the micromanipulator. In this study, a new asymmetric cable-driven type of micromanipulator for a surgical robot was designed, and a joint angle estimator (JAE) was designed based on the dynamical model of the single cable-driven joint. Closed-loop control of the joint angle was carried out by regarding the JAE output as the feedback signal. On this basis, an external force estimator was designed using a disturbance observer (DOB). The experimental results show an average accuracy of the joint angle estimator of about -0.150° , with excellent control precision, the largest absolute error of about 0.95° , and an average error of 0.175° . The accuracy of the force estimator was at a high level during static loading. The estimated accuracy was 94% at external force is greater than 1 N, and the estimated accuracy was 82% for an external force of 0.3 N. These results predict that force sensing of a cable-driven micromanipulator in this paper can used to realize the micromanipulator's force feedback of a minimally invasive surgical robot.

1 Introduction

With the development of robot technology, robot-assisted surgery has been widely applied. ZEUS (Haidegger and Benyo, 2008) and the Da Vinci (Monsarrat et al., 2009) are the two most successful systems of a minimally invasive surgery robot (MISR). Most problems encountered during early clinical procedures have been solved. However, a major deficiency of MISR is the lack of force-sensing information feedback. The lack of this information may result in significant harm and trauma to normal tissue (Tholey et al., 2005). It is difficult to apply accurate operating force to tissue during accurate operations, such as separation and suture. The force sensing for MISR systems is an active research subject, as improved force sensing will improve surgical operation skills and the quality of the procedure (Ortmaier et al., 2007). Specifically, force sensing improves the performance and efficiency of MISR systems by reducing the contact force peak and decreasing the task execution time (Okamura et al., 2011).

The force estimation methods for MISR systems can be roughly divided into direct detection and indirect detection methods based on electric resistance or fiber and the displacement of the actuator input, respectively (Fu et al., 2014). Yin and Guo (2016) designed a teleoperated robotassisted catheter operating system with haptic. The sensors for force sensing include strain gauge-based force sensors, piezo-resistive force sensors, capacitive force sensors, piezo magnetic force sensors, optical force sensors, vision-based force sensors, and electroactive force sensors, among others (Ma et al., 2014; Wei and Xu, 2015). Strain gauge is the most commonly used force detecting element. In order to realize the precise measurement of force, strain gauges are typically put on the elastomer. If an external force is applied on the elastomer, the resistance of the strain gauge and the electricity bridge voltage will be changed, so the external force can be detected by measuring the changes in the resistance bridge output voltage. Brown (2002) developed a motor driven grasping apparatus and measured the force and organizational characteristics using a strain gauge. It is important to reduce friction to improve the accuracy of force detection because the detecting element is far away from the point of interaction forces. Some researchers such as Mayer et al. (2008), Prasad et al. (2003), Kuebler et al. (2005) measured the instrument's force directly using micro-force sensors installed in the manipulator's end. Because the grating sensor has good magnetic resonance, Peirs (2004), and Puangmali et al. (2012) developed a three-dimensional force detection unit based on the use of grating. Lim (2014) realized the clamping force test by installing a grating sensor in the forceps of a micromanipulator. Xie (2015b) developed a new contact two-dimensional force sensor used in flexible micro devices based on optical fiber, with accuracy that can reach 83 %. Zhang et al. (2017) evaluated the performance of a strain-gauge force sensor for a haptic robotassisted catheter operating system. Xu (2015) designed a novel compliant gripper with integrated position and grasping/interaction force sensing. Xie et al. (2016) researched the array platform for robotic cell microinjection force measurement. Conductive polymer materials can also be used to manufacture detecting elements. The researchers (Valdastri et al., 2006) of Verimetra Company has pursued microfabrication technology to design intelligent surgical instruments. They used the instrument itself as a substrate to create a semiconductor strain gauge, in which the strain gauge was embedded on the surface of the forceps or knives. However, this equipment has only been used in a small range, since the MISR instrument is a compact construction, and it is unsuitable to install sensors in the end of a manipulator because of the need for sterility. Additionally, surgical instruments are consumable, thus increasing the operation cost.

One of the simplest ways to detect force is to detect the displacement changes of the elastic element. Rosen et al. (1999) designed a teleoperation endoscopic gripper with force feedback. Comparison of the position reference input and the actual position allows the generation of a position error when the gripper clamps human tissue and a clamping force will be automatically detected during operation. Friction and mechanical clearance can cause a position error, or a torque estimation error. Tholey (2004) realized indirect measurement of clamping force by detecting the motor current. The measurement error is big in this system due to the mechanism. Zhao (2015) realized the force estimate of micro device through a motor current, but the accuracy is too low when the external force is less than 2 N. Haraguchi (2016) developed a micro device with 4 DOFs and estimated the force information of the micro device using a neural network. Hongbing Li (2013) realized the force testing of a 3 DOF micro instrument based on a disturbance observer, with a minimum resolution of 0.5 N.

In conclusion, the cost of direct force measuring is high and the limitations are obvious. The cost is low with good



Figure 1. The three different basic cable-driven mechanisms.

adaptability if an integrated sensor in the end of the micro device driving mechanism is used to measure cable tension and estimate the external forces of the micromanipulator indirectly based on motion control and drive information. Overall, indirect force detection can avoid several problems and the development of an indirect force detection method for the micromanipulator of a surgical robot based on a disturbance observer is the focus of this study.

The remainder of this paper is organized as follows. The cable-driven micromanipulator and the single joint principle prototype are described in Sect. 2. The dynamics, closed loop control of the finger angle based on the angle estimator and force detection method based on disturbance observer are proposed in Sect. 3, the experimental results of motion control and force detection are shown in Sect. 4. Conclusions and future works are provided in Sects. 5 and 6, respectively.

2 The cable-driven micromanipulator and the single joint principle prototype

2.1 The cable-driven system mechanism

The torque generated by a motor is transmitted through a flexible cable in a cable-driven system. The force or torque in two different directions is required to drive a rotational joint, but the cable cannot transmit forces in the pushing direction. Three different basic cable-driven mechanisms have been used to satisfy these requirements, as shown in Fig. 1.

As shown in Fig. 1a, the mechanism can drive one joint with one motor. The structure is simple, so it is widely used in many robotic manipulators. However, sometimes it is difficult to ensure that the non-pulled side is tensioned, which will cause backlash and slow responses. This will seriously affect the performance of the mechanism, so it is essential to add a pre-tensioning mechanism, which will add to the complexity of the system.

In the second mechanism, shown in Fig. 1b, each cable is independently driven by one motor. This mechanism provides high performance and it is easy to design the cable routing structure. The joint stiffness can be easily adjusted



Figure 2. (a) Cable-driven mechanism of the micromanipulator. (b) The 3-D model of the micromanipulator wrist.



Figure 3. 3-D model of the single joint prototype.

by controlling the two motors. However, the cost is higher, as the number of required motors is doubled compared with other mechanisms, and application is limited by the requirement of compact space.

As is shown in Fig. 1c, the third mechanism uses a spring for the reversed actuation of one side, and a motor is used to drive the other side. The cables can be tensioned by pulling the spring to an appropriate distance. This will apply two directional forces to the joint. The cable tension can always be maintained without an additional pre-tensioning mechanism. Due to simple cable routing, the appropriate cost and the character of the tensioning itself makes the spring-motor mechanism a good choice when compact structures are required.

From the analysis above, the spring-motor mechanism (shown in Fig. 2c) was selected for the design of the micro-manipulator.

2.2 The cable-driven micromanipulator for surgical robot

The mechanism of the micromanipulator for a surgical robot is shown in Fig. 2a. The four different colours represent the drive mechanism of different joints, with each joint designed based on the spring-motor mechanism. The micromanipulator has four DOFs, and the wrist of the micromanipulator has 3 DOFs, consisting of one pitch joint and two deflection joints. The driving force of each joint is determined by the difference between the tensions of the cables in each loop of the joint cable routing. The opening, closing, and deflection of the wrist are determined by the different combinations of the rotation directions of the motors used in gripper A and gripper B. The 3-D model of the wrist is shown in Fig. 2b. The wrist and the driven components are driven by a rotary joint. The components of each joint are similar to those of the single joint prototype, as shown in Fig. 3.

2.3 The force analysis of the micromanipulator

The dynamic equation of operating forceps is shown in Eq. (1) and takes the external force of the system and the joint friction torque into consideration.

$$\boldsymbol{\tau}_{i} = \mathbf{D}_{i}(\boldsymbol{q})\boldsymbol{\ddot{q}} + \boldsymbol{H}_{i}(\boldsymbol{q},\boldsymbol{\dot{q}}) + \boldsymbol{G}_{i}(\boldsymbol{q}) + \boldsymbol{\tau}_{fi} + \mathbf{J}_{i}^{\mathrm{T}}\boldsymbol{F}_{\mathrm{ext}}^{i}.$$
 (1)



Figure 4. The mechanism model diagram of the single joint principle prototype.

Where i = a, b, a and b represent gripper A and gripper B respectively. τ_i , $\mathbf{D}_i(q)$, $H_i(q,\dot{q})$, $G_i(q)$, τ_{fi} , $\mathbf{J}_i^{\mathrm{T}}$ and F_{ext}^i are the joint driven torque, inertia matrix, centrifugal force and Coriolis force, gravity, friction torque, force Jacobian matrix and external force respectively. The driving torque of each joint is shown in Eq. (2); the meaning of the superscript *i* is similar to Eq. (1). Where, F_{M} is the tension of the positive driven cable. F_{S} is the tension of the negative driven cable.

$$\tau_{1} = r_{1} \left(F_{M}^{r} - F_{S}^{r} \right)
\tau_{2} = r_{2} \left(F_{M} - F_{S} \right)
\tau_{3}^{i} = r_{3} \left(F_{M}^{i} - F_{S}^{i} \right)
\tau_{i} = \left[\tau_{1} \tau_{2} \tau_{3}^{i} \right]^{T}.$$
(2)

When the external force is zero, the micromanipulator moves freely. The dynamic equation of the operating forceps is shown in Eq. (3), and the parameters can be obtained by inverse dynamics identification.

$$\hat{\boldsymbol{\tau}}_{i} = \left[\hat{\tau}_{1}\hat{\tau}_{2}\hat{\tau}_{3}^{i}\right]^{\mathrm{T}} = \hat{\boldsymbol{D}}_{i}(\boldsymbol{q})\boldsymbol{\ddot{q}} + \hat{\boldsymbol{H}}_{i}(\boldsymbol{q},\boldsymbol{\dot{q}}) + \hat{\boldsymbol{G}}_{a}(\boldsymbol{q}) + \hat{\boldsymbol{\tau}}_{fi}.$$
 (3)

When the external force is not equal to zero, the external force can be obtained from Eq. (4), where τ_i is the actual joint torque and $\hat{\tau}_i$ is computed by the parameters in Eq. (3). Digital filtering can be used first to obtain the data of τ_i and $\hat{\tau}_i$.

$$\boldsymbol{F}_{\text{ext}}^{i} = \mathbf{J}_{i}^{-T} \left(\boldsymbol{\tau}_{i} - \hat{\boldsymbol{\tau}}_{i} \right).$$
(4)

The external force F_{ext} applied on the micromanipulator and the clamping force F_{cp} of the micromanipulator can be described as in Eq. (5).

$$F_{\text{ext}} = F_{\text{ext}}^{a} + F_{\text{ext}}^{b}$$

$$F_{\text{cp}} = \frac{1}{2} \left(\left| F_{\text{ext}}^{ya} \right| + \left| F_{\text{ext}}^{yb} \right| \right).$$
(5)

2.4 The prototype of the micromanipulator based on a single joint model

The four joints drive the micro devices and the cable routing structure as presented in the analysis above. The performance of the single joint principle prototype can illustrate the performance of the micromanipulator. The prototype of the single joint model was designed as shown in Fig. 3. The DC servo motor provides the positive driving force and the return spring provides the negative driving force. The displacements of the flexible cables were measured by two sets of raster detection modules and a non-contact micro magnetic encoder was used to detect the joint angle of the gripper. A photoelectric switch provides the origin signal of the system.

3 The force estimates research of the cable-driven micromanipulator prototype

3.1 The dynamic model and the joint angle estimator of the single joint prototype

The mechanism model diagram of single joint principle prototype is shown in Fig. 4. The model can be divided into six parts. Because the flexible cable moves at a low speed, highfrequency tremors are negligible, and the model of flexible cable is equivalent to a mass-spring-damper model. Motor movement cannot be completely passed to the slider. The displacement of slider 1 and the positive driving cable is determined by the detection value of grating ruler component 1, and the displacement of slider 2 and the negative driving cable is determined by the detection value of grating ruler component 2. The friction influence of the subsystems should be considered, and the gravitational effect of the gripper can be ignored since the gravity direction of the gripper direction and rotation direction are both vertical.

The dynamic equilibrium equations were established individually, as is shown below. When the system is in the original position, the flexible cables are in astatic state, and the joint angle and the displacement of sliders are zero. The relationship of the initial tensioning force of the positive driving cable and the negative driving cable are shown in Eq. (6), and F_0 is the initial tension of the system.

$$F_{w10} = F_{w20} = F_0. ag{6}$$



Figure 5. The basic block diagram of DOB.



Figure 6. The external force estimator for the single joint system model based on DOB.

The model of part 1 is shown in Eq. (7), where, i_m is the motor armature current, F_1 is the load of the rope wheel, τ_1 is the load torque, τ_m is the input torque, z_i is the reduction ratio, r_m is the effective radius of the rope wheel, K_m is the torque constant, J_m is the effective moment of inertia of the DC motor, B_m is the viscous damping constant, $\ddot{\varphi}$ and $\dot{\varphi}$ are the angular acceleration and angular velocity of the motor, respectively.

$$\begin{aligned}
\tau_{\rm m} &-\tau_{\rm l} = J_{\rm m} \ddot{\varphi} + B_{\rm m} \dot{\varphi} \\
\tau_{\rm m} &= K_{\rm m} i_{\rm m} \\
\tau_{\rm l} &= \frac{r_m}{z_i} F_{\rm l}.
\end{aligned}$$
(7)

The model of the guide-slider and the idler component 1 (part 2) is shown below, where F_{w1} is the cable tension that drives the gripper joint, m_0 is the mass of slider 1, \ddot{x}_1 is the slider acceleration, τ_{f1} is the equivalent friction of part 2 and



Figure 7. Experimental design of the single joint prototype system.

is composed of viscous friction and coulomb friction, f_{sv1} and f_{sc1} are the coulomb friction coefficient and the viscous friction coefficient, respectively, $sgn(\cdot)$ is the symbolic function, and \dot{x}_1 is the slider velocity.

$$F_{1} - F_{w1} = m_{0}\ddot{x}_{1} + \tau_{f1}$$

$$\tau_{f1} = \tau_{f1_{sv}} + \tau_{f1_{sc}} = f_{sv1}\dot{x}_{1} + f_{sc1}\text{sgn}(\dot{x}_{1}).$$
(8)

As the mass of the positive driving cable is very small, the viscous friction coefficient $B_w = 2\xi_w \sqrt{m_1 K_w}$, and the influence of viscous friction and mass can be ignored to simplify the model. The model of the positive driving cable (part 3) can be regarded as a spring model, as is shown in Eq. (9). K_w is the elastic coefficient of the positive driving cable and y_1 is the displacement of one side of the positive driving cable, which is fixed to the gripper joint.

$$F_{w1} = K_{w1}(x_1 - y_1) + F_{w10}.$$
(9)

The model of the spring (Sect. 4) is shown in Eq. (10). F_2 is the spring tension, K_s is the elastic coefficient of the spring, and x_2 is the displacement of the spring mobile side.

$$F_2 = K_{\rm s} x_2 + F_{\rm w20}. \tag{10}$$

Similarly to part 2, the model of the guide-slider and idler component 2 (part 5) is shown in Eq. (9), and the variables in Eq. (11) are defined as in part 2.

$$\begin{cases} F_{w2} - F_2 = m_0 \ddot{x}_2 + \tau_{f2} \\ \tau_{f2} = \tau_{f2_{sv}} + \tau_{f2_{sc}} = f_{sv2} \dot{x}_2 + f_{sc2} \text{sgn}(\dot{x}_2). \end{cases}$$
(11)

Similarly to part 4, the model of the negative driving cable (part 6) is shown in Eq. (12), and the variables in Eq. (12) are defined as in Eq. (9).

$$F_{w2} = K_{w2}(y_2 - x_2) + F_{w20}.$$
 (12)



Figure 8. Control block diagram of the parameter identification for the joint angle estimator.

The dynamic model of the gripper joint (part 7) is shown in Eq. (13), where, θ , τ_e , m_e , J_e and r are the gripper joint angle, joint driven torque, joint effective mass, joint equivalent moment of inertia, and the effective radius of the cable tension, respectively. τ_{ef} is the friction torque of the joint and is composed of the viscous friction torque and the coulomb friction torque τ_{ext} is the external force moment, and l_e is the effective radius of the external force F_{ext} .

$$\tau_{e} = J_{e}\dot{\theta} + \tau_{ef} + \tau_{ext}$$

$$\tau_{e} = (F_{w1} - F_{w2})r$$

$$\tau_{ef} = \tau_{efv} + \tau_{efc} = f_{efv}\dot{\theta} + f_{efc}\text{sgn}(\dot{\theta})$$

$$\tau_{ext} = F_{ext}l_{e}.$$
(13)

The relationship between the joint angle θ and y_1 , y_2 is shown below, y_1 is the displacement of the positive driving cable which is fixed on the gripper, and y_2 is the displacement of the negative driving cable.

$$y_1 = y_2 = r\theta. \tag{14}$$

Combining Eqs. (6), (11), (12), and (14), the two different expressions of F_{w2} can be obtained, as shown below.

$$\begin{bmatrix} F_{w2} = K_{w2}r\theta - K_{w2}x_2 + F_0 \\ F_{w2} = m_1\ddot{x}_2 + f_{sv2}\dot{x}_2 + f_{sc2}\text{sgn}(\dot{x}_2) + K_sx_2 + F_0. \end{bmatrix}$$
(15)

Then the relationship between x_2 and θ can be found as shown in Eq. (16). Equation (16) is the overall model of the joint angle estimator. The parameter identification and the practical application will be demonstrated in the experimental section.

$$\theta = \frac{m_1}{K_{w2}r} \ddot{x}_2 + \frac{f_{sv2}}{K_{w2}r} \dot{x}_2 + \frac{f_{sc2}}{K_{w2}r} \operatorname{sgn}(\dot{x}_2) + \frac{K_s + K_{w2}}{K_{w2}r} x_2.$$
(16)

3.2 The force estimator of the single joint principle prototype based on DOB

The DOB regards the difference between the actual output and the output of the dynamic model (without external force) as a disturbance applied on the system. When an external force is applied, the equivalent disturbance includes not only the modelling uncertainties but also the external force information. Therefore, force estimation based on the DOB must find the external force information from the equivalent disturbance. The advantage of the DOB is that it does not need force sensors or other sensors to estimate the external force. The DOB is designed to achieve the external force detection of the joint prototype system. The dynamics of a motor are described by the following equation.

$$\begin{cases} J_{\rm m}\ddot{\varphi} = f_d + K_{\rm m} i_{\rm m}^{\rm ref} \\ f_d = \tau'_{\rm dis} + B_{\rm m}\dot{\varphi}. \end{cases}$$
(17)

Where: $J_{\rm m}$, $B_{\rm m}$, φ , $i_{\rm m}^{\rm ref}$ and $K_{\rm m}$ denote the inertia mass, damping coefficient, position response, current, and the force coefficient of the motor, respectively. f_d denotes the motor load, and is composed of damping and disturbance, and the disturbance includes the external force. The basic block diagram of the DOB is shown in Fig. 5, where $J_{\rm mn} = J_{\rm m}$, and $g_{\rm dis}$ is the parameter of the low-pass first order filter $\frac{g_{\rm dis}}{s+g_{\rm dis}}$. If $\tau_{\rm dis1} = 0$, the damping and disturbance are estimated using the low-pass first order filter as in the following equation.

$$\hat{f}_d = \frac{g_{\rm dis}}{s + g_{\rm dis}} f_d. \tag{18}$$

When the external force F_{ext} is applied on the end of the gripper, the load of the rope wheel fixed on the motor is F_1 . If there is no external force applied on the end of the gripper, the load of the rope wheel fixed on the motor is F'_1 and the relationship of F_1 and F'_1 is as shown below.

$$F_1 = F'_1 + F_{\text{ext}}r.$$
 (19)

The external force estimator for the single joint principle prototype system is designed as shown in Fig. 6. The output of the external force estimator is shown below.

$$\hat{F}_{\text{ext}} = \frac{g_{\text{dis}}}{s + g_{\text{dis}}} (f_d - \hat{f}_d).$$
⁽²⁰⁾

Where $f'_d = \hat{F}'_1 r_m / z_i + \hat{B}_m \dot{\varphi}$. To estimate the external force, the models of \hat{F}'_1 and \hat{B}_m must be known. The identification models of \hat{F}'_1 and \hat{B}_m are shown in the next part.

3.3 The identification models of $\hat{B}_{\rm m}$ and $\hat{F}_{\rm 1}$

When the motor is running with no load, $f_d = B_m \dot{\phi}$, and $\tau_{dis1} = 0$. The output of Fig. 5 is $\hat{f}_d = \hat{B}_m \dot{\phi}$, and Fig. 5 is the motor damping estimator. Parameter \hat{B}_m is a constant that can be obtained by the least square method.

When the single joint principle prototype system runs without applied applied on the end of the gripper ($F_{\text{ext}} = 0$), let $\tau_{\text{dis1}} = \hat{B}_{\text{m}}\dot{\varphi}$, and $f_d = F'_1 r_{\text{m}}/z_i + B_{\text{m}}\dot{\varphi}$. Then, the output



Figure 9. Identification result of the joint angle estimator model.



Figure 10. The performance of the control system without a joint angle estimator.

of disturbance observer in Fig. 5 is $\hat{f}_d = \hat{F}'_1 r_m / z_i$, and then \hat{F}' can be determined by the equation below.

$$F'_1 = \hat{f}_d z_i / r_{\rm m}.$$
 (21)

When the external force F_{ext} is applied on the end of the gripper, we must get the estimated value of F'_1 from the information we obtain on the state of the gripper contacting the environment. If the system is running without the application of external force on the gripper ($F_{\text{ext}} = 0$), the relationship of F'_1 and F_1 is $F_1 = F'_1$. The three models of F'_1 were established by dynamic analysis of the single joint prototype system.

Model A: the model is established based on the dynamics analysis of part 2 and part 3. Combined Eqs. (6), (8) and (9), the expression of F'_1 is shown below.

$$F_1' = m_0 \ddot{x}_1 + f_{sv1} \dot{x}_1 + f_{sc1} \operatorname{sgn}(\dot{x}_1) + K_{w1} x_1 - K_{w1} r \theta + F_0.$$
(22)

Model B: the model is established based on the dynamic analysis of part 2, part 6, and part 7. Combining Eqs. (6), (8) and (12), (13) and (14), the expression of F'_1 is shown

below.

$$F_{1}' = \frac{J_{e}}{r}\ddot{\theta} + \frac{f_{efv}}{r}\dot{\theta} + \frac{f_{efc}}{r}\mathrm{sgn}(\dot{\theta}) + K_{w2}r\theta + m_{0}\ddot{x}_{1} + f_{sv1}\dot{x}_{1} + f_{sc1}\mathrm{sgn}(\dot{x}_{1}) + m_{1}\ddot{x}_{2} + f_{sv2}\dot{x}_{2} + f_{sc2}\mathrm{sgn}(\dot{x}_{2}) - K_{w2}x_{2} + F_{0}.$$
(23)

Model C: the model is established based on the dynamic analysis of parts 2, 4, 5 and 7. Combining Eqs. (6), (8), (10), (11), (13) and (14), the expression of F'_1 is shown in Eq. (24).

$$F_{1'} = \frac{J_{\rm e}}{r}\ddot{\theta} + \frac{f_{\rm efv}}{r}\dot{\theta} + \frac{f_{\rm efc}}{r}{\rm sgn}(\dot{\theta}) + m_0\ddot{x}_1 + f_{\rm sv1}\dot{x}_1 + f_{\rm sc1}{\rm sgn}(\dot{x}_1) + m_1\ddot{x}_2 + f_{\rm sv2}\dot{x}_2 + f_{\rm sc2}{\rm sgn}(\dot{x}_2) + K_{\rm s}x_2 + F_0.$$
(24)

The actual value of F'_1 and f_d can be determined by the output of Fig. 5, as shown in the analysis above. The identification experiment and identified value of the model parameters are described in the next section.

4 Experimental research

The experimental system is shown in Fig. 7, and the specifications are listed in Table 1. Encoder information acquisition of the motion control card (Leisai DMC2610) was used to acquire the displacements of grating scales and the angle of the gripper. The driving force arm of the gripper joint is 4 mm, and the length of the gripper is 20 mm. The external force was applied by loading weights, using Labview software and a Microsoft windows XP operating system.

4.1 Parameter identification and the performance of the joint angle estimator

In order to identify the parameters of the joint angle estimator, a micro magnetic encoder was used to detect the actual angle of only the gripper joint. The micro magnetic encoder has no effect on the control. The angle of the motor was used as the feedback signal. In other words, the motor was under closed-loop control, but the gripper joint angle was controlled by open-loop control, as shown in Fig. 8. The gripper angle θ can be obtained through the micro magnetic encoder, and x_2 can be obtained using the grating ruler. Then, the parameters of the joint angle estimator model can be identified by the least squares method. The identification model is shown below. The meaning of the parameters ρ_s in Eq. (25) is the error vector.

$$Y_s = W_s \chi_s + \rho_s \tag{25}$$

$$\begin{cases} Y_{s} = \theta, W_{s} = \begin{bmatrix} \hat{x}_{2} & \hat{x}_{2} & \text{sgn}(\hat{x}_{2}) & x_{2} \end{bmatrix} \\ \chi_{s} = \begin{bmatrix} \frac{m_{1}}{K_{w2}r} & \frac{f_{sv2}}{K_{w2}r} & \frac{f_{sc2}}{K_{w2}r} & \frac{K_{s} + K_{w2}}{K_{w2}r} \end{bmatrix}^{\text{T}}. \end{cases}$$
(26)

Where, x_2 is the position detected value of the Grating ruler component 2, \dot{x}_2 is the speed, and \ddot{x}_2 is the acceleration, and sgn (\dot{x}_2) is the symbolic function.



Figure 11. The control block diagram with a joint angle estimator.

Table 1. Specifications of the experiment system.

Specifications	
Motor	Maxon RE25 20 W, incremental
	photoelectric encoder: 1000p/r,
	Reduction ratio 35 : 1
Servo drive	Copley ACI-055-18
Grating reading head	Renishaw :RH100X30D05A
	Resolution: 0.001 mm
Grating ruler	RGS-40
Micro magnetic encoder reading head	Renishaw :RM08ID0012B02L2G00(4096 p/r)
	Resolution: 0.001 mm
Micro magnetic encoder magnetic bead	RMM44A3A00
Guide rail and slider	MISUMI SSEBZ8L-85
Spring	KSSC2189 0.6566 N mm ⁻¹



Figure 12. The performance the control block diagram with a joint angle estimator.

Through the identification experiment, the parameters vector can be determined, as shown below.

$$\hat{\boldsymbol{\chi}}_{s} = [0.0805 \ 0.5225 \ 0.0025 \ 264.3560]^{\mathrm{T}}.$$

The actual data, the identification result of the joint angle, and the errors are shown in Fig. 9. The average of the identification error is 0.2750° the maximum identification error



Figure 13. The test results of the robustness of the control system.

is 0.8355° , and the minimum of the identification error is -0.8321° . These values indicate good accuracy of the joint angle estimator.

The performance of the general control system is shown in Fig. 10. There was significant error between the desired trajectory and the actual trajectory. The average error was



Figure 14. The identification experimental result of motor viscous damping.



Figure 15. The verification experimental result of motor viscous damping.

 1.912° , the maximum error was 4.134° , and the minimum was 0.964° . The performance does not the requirements for micro devices of precise operation.

In order to verify the performance of the joint angle estimator, a control system was designed and is shown in Fig. 11. The output of the joint angle estimator is the feedback signal of the position loop, the position control is a PD control and the speed control is a PI control. The parameters can be set through the servo drive. The parameters of the controller are shown below.

Position loop: $\begin{bmatrix} K_{p1} & K_{D1} \end{bmatrix} = \begin{bmatrix} 98 & 14 \end{bmatrix}$ Speedloop: $\begin{bmatrix} K_{vp} & K_{vi} \end{bmatrix} = \begin{bmatrix} 100 & 40 \end{bmatrix}$.

The desired trajectory and the actual trajectory are shown in Fig. 12. When the gripper joint is driving with no external force, the desired trajectory, the actual trajectory, and the estimated trajectory are almost the same. The average error between the desired trajectory and the actual trajectory was -0.150° , the maximum error was 0.905° , and the minimum error was -0.974° . The average error between the actual trajectory and the estimated trajectory was 0.170° , the maximum error was 0.715° , and the minimum was -0.498° . Overall, the control precision of the system is higher than the



Figure 16. The identification results and the identification errors of the three models.



Figure 17. The identification result of the simplified model C.

system without a joint angle estimator. In other words, the joint angle estimator works well and the necessary precision can be obtained.

To test the robustness of the control system, a complex trajectory was used to assess the performance of the control system and the joint angle estimator when an external force of 2.5 N was applied on the gripper. The experimental result is shown in Fig. 13. The average error between the desired trajectory and the actual trajectory is -0.105° . The maximum error is 1.202° , and the minimum is -1.271° . The average error between the actual trajectory and the estimated trajectory is 0.076° , the maximum error is 0.508° , and the minimum error is -0.454° . These values indicted excellent robustness of the control system and the joint angle estimator.



Figure 18. The verification result of the simplified model C.



Figure 19. External force estimation experimental system.

4.2 The identification experiment of $\hat{B}_{\rm m}$ and $\hat{F'}_{1}$

The motor was controlled without applied load on the motor output shaft, so that the actual output torque \hat{f}_d can be obtained according to Fig. 5, and $\dot{\varphi}$ can be obtained from the motor encoder. The relationship between \hat{f}_d and $\dot{\varphi}$ is $\hat{f}_d = B_{\rm m}\dot{\varphi}$ can be determined and then the parameter $B_{\rm m}$ can be calculated by the least square method. The identification value of $B_{\rm m}$ is $1.6934 \times 10^{-5} \,\rm Nm \, rad^{-1}$. The identification experimental result is shown in Fig. 14, and the verification experimental result is shown in Fig. 15. The result shows good precision of the identification of motor viscous damping.

The identification experiment was performed based on the joint angle closed-loop control by regarding the joint angle estimator output as the feedback signal. The control block diagram is shown in Fig. 11. The actual value of F'_1 can be obtained as described in the analysis in Sect. 3.3. The values of the observation matrixes can be obtained by reading the grating sensors and the micro magnetic encoder. The three different models of F'_1 are shown in Sect. 3.3, where the model C can be represented by the following expression,



Figure 20. Negative direction loading experiment results at 0°.



Figure 21. Positive direction loading experiment results at 0°.

where x_1 is the position detected value of the grating ruler component 1, \ddot{x}_1 , \dot{x}_1 and sgn(\dot{x}_1) are acceleration, speed and symbolic function, respectively. The other models can similarly be written as expressions. The parameter matrixes of the three models can be obtained, and the identification results and the identification errors are shown in Fig. 16.

$$Y_{\rm c} = W_{\rm c} \chi_{\rm c} + \rho_{\rm c} \tag{27}$$

$$\begin{array}{l} Y_{\rm c} = F'_{\rm L} \\ W_{\rm c} = \begin{bmatrix} \ddot{\theta} \ \dot{\theta} \ \operatorname{sgn}(\dot{\theta}) \ \ddot{x}_1 \ \dot{x}_1 \ \operatorname{sgn}(\dot{x}_1) \ \ddot{x}_2 \ \dot{x}_2 \ \operatorname{sgn}(\dot{x}_2) \ x_2 \ 1 \end{bmatrix} \\ \chi_{\rm c} = \begin{bmatrix} J_{\rm e}/r \ f_{\rm efv}/r \ f_{\rm efc}/r \ m_0 \ f_{\rm sv1} \\ f_{\rm sc1} \ m_1 \ f_{\rm vp2} \ f_{\rm cp2} \ K_{\rm s} \ F_0 \end{bmatrix}^{\rm T}. \end{array}$$

The cable tension F'_1 will have a larger error when the joint velocity is zero because the system has a hysteresis effect. The movement of the motor cannot be passed to the gripper immediately as the cable is not a rigid body. When the joint velocity is non-zero the identification results are trustworthy. The average errors of the three models are -0.0228, 0.0189, and -0.0063 N respectively. The identification precision of model C is higher than that of the others,



Figure 22. The partition of the experimental results curve.



Figure 23. Negative direction loading experiment results at 30°.

so model C was adopted for further studies. The parameters and their standard variance are shown below.

 $\hat{\boldsymbol{\chi}}_{c} = \begin{bmatrix} \hat{\boldsymbol{\chi}}_{c1} & \hat{\boldsymbol{\chi}}_{c2} & \hat{\boldsymbol{\chi}}_{c3} & \hat{\boldsymbol{\chi}}_{c4} & \hat{\boldsymbol{\chi}}_{c5} & \hat{\boldsymbol{\chi}}_{c6} & \hat{\boldsymbol{\chi}}_{c7} & \hat{\boldsymbol{\chi}}_{c8} & \hat{\boldsymbol{\chi}}_{c9} & \hat{\boldsymbol{\chi}}_{c10} & \hat{\boldsymbol{\chi}}_{c11} \end{bmatrix}^{\mathrm{T}} \\ = \begin{bmatrix} 0.1975 & -9.808 & 0.005 & -38.64 & 6705 & 3.259 & 38.99 \\ -4404 & 5.436 & 669.0 & 19.53 \end{bmatrix}^{\mathrm{T}} \\ \% \boldsymbol{\sigma}_{\hat{\boldsymbol{\chi}}_{c}} = \begin{bmatrix} 32.29 \% & 27.3 \% & 2625 \% & 59.23 \% & 7.678 \% & 3.809 \% \\ 54.14 \% & 15.26 \% & 2.518 \% & 1.932 \% & 0.115 \% \end{bmatrix}.$

As the velocity and acceleration of the system are small and the standard variance of χ_{c1} , χ_{c2} , χ_{c3} , χ_{c4} , χ_{c5} , χ_{c7} and χ_{c8} are over 5%, so the influence of these parameters can be ignored. The simplified model C is shown below.

$$Y_p = W_p \chi_p + \rho_p, \tag{28}$$

$$\begin{cases}
Y_p = \hat{F}'_L \\
W_p = [sgn(\dot{x}_1) \ sgn(\dot{x}_2) \ x_2 \ 1] \\
\chi_p = [f_{sc1} \ f_{cp2} \ K_s \ F_0]^T.
\end{cases} (29)$$

The parameters of the simplified model C can be obtained through the LS method. The identification result of the simplified model C is shown in Fig. 17, and the values of the parameters and their standard variance are shown below. Another experiment was used to verify the simplified model C, as shown in Fig. 18. The average error was 0.011 N. The above analysis illustrated the accuracy of the simplified



Figure 24. Positive direction loading experiment results at 30°.



Figure 25. Positive direction loading experiment results at -40° .

model, suggesting the model can be used to estimate the external force applied on the gripper by the method presented in Fig. 6.

 $\hat{\chi}_p = [3.879 \ 5.027 \ 707.7 \ 19.52]^{\mathrm{T}}$ % $\boldsymbol{\sigma}_{\hat{\chi}_c} = [3.025 \ \% \ 2.658 \ \% \ 1.787 \ \% \ 0.115 \ \%].$

4.3 The external force estimation experiment

The external force estimation strategy is shown in Fig. 6 in which the gripper was controlled by the method shown in Fig. 11. $f'_d = \hat{F}'_1 r_m/z_i + \hat{B}_m \dot{\varphi}$ can be determined using the identification models in Sect. 4.1. External force applied on the gripper is shown in Fig. 19. The external force estimation experiments were performed by applying external forces on the gripper of different magnitudes and in different directions. The positive direction and negative direction external forces of 30, 50, 100, 200, and 250 g were tested. The experiment results are shown in Figs. 20 to 26.

The experimental results for a joint angle of 0° are shown in Figs. 20 and 21. Fig. 22a shows the experimental process when the external force is 2 N: (1) is the no-load region, (2) is the loading process, and (3) is the stable region. The no-load



Figure 26. Positive direction loading experiment results at -40° .

error range of the external forces estimation is about ± 0.1 N, with high accuracy of the force estimator. The estimated accuracy can reach up to 94 % for an external force greater than 1 N, and the estimated accuracy can reach 82 % for an external force of 0.3 N. The external force has little influence on the joint angle control precision. The greatest error was 1.25° for an external force of 2.5 N.

An experimental process is shown in Fig. 22b for a joint angle of 30 and -40° : (1) is the moving process, (2) is the adjustment process, (3) is the no-load region, (4) is the loading process, and (5) is the stable region. The dynamic noload error is about ± 0.15 N when external forces are applied on the positive direction. The dynamic no-load error is about ± 0.2 N when external forces are applied on the negative direction. The static no-load error is about ± 0.15 N, with good accuracy of the force estimator. The estimated accuracy can reach 95 % when the external force is more than 1 N, and the estimated accuracy can reach 84 % when the external force is 0.3 N. The external force has little influence on joint angle control precision. The greatest error was 1.4°, when external force was applied to the gripper.

5 Conclusions

A new asymmetric cable-driven type of micromanipulator for surgical robot was described. Using a single joint sample machine to verify the validity of the method proposed in this paper, a joint angle estimator was designed (JAE) based on the dynamical model of the single cable-driven joint. The average accuracy of the joint angle estimator was measured at about 0.2750°, with a maximum error of 0.8355°. The closed-loop control problem of the joint angle was solved by considering the joint angle estimator output as the feedback signal. The biggest tracking error was measured at about $\pm 0.9^{\circ}$. We designed the external force estimator using the method of disturbance observer, and the model parameters were identified and external force estimation experiments were performed. The experimental results shown that the static no-load error was about ± 0.1 N and the dynamic loading error was about ± 0.15 N. The precision of the external force estimator can reach up to 94 % when the external force is more than 1 N, and the precision can reach 84 % at an external force of 0.3 N. In summary, the external force estimation method presented in this paper is effective and accurate, and can be used to realize force feedback for a minimally invasive surgical robot.

We will aim at realizing the external force estimation of the 4 DOFs micro device. Additionally, the hybrid control of position and force will be researched and let the surgeon feel the external force.

Data availability. All the data for this paper are given in the form of and figures, and can be obtained by requesting from the corresponding author.

Competing interests. The authors declare that they have no conflict of interest.

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