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A simple design rule for 1st order form-closure of underactuated hands

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Abstract. The property of form-closure of a grasp, as generally defined in the literature, is based on the assumption that contact points between the hand and the object are fixed in space. However, this assumption is false when considering a grasp exerted by an underactuated hand, since in this case, it is not possible to control the position of each phalanx independently. In spite of researchers' interest in studying form-closure, none of the available published work on this subject takes into consideration the particular kinematics of underactuated hands. Actually, there are few available tools to qualify or quantify the stability of a grasp exerted by an underactuated hand, thus the design of underactuated hands mostly results from an intuitive approach. This paper aims to reduce this gap.

A classification of underactuated hands is proposed, based on the expression of contact forces. This highlights the influence of non-backdrivable mechanisms introduced in the transmission of the closing motion of the hand on the stability of the grasp. The way to extend the original definition of form-closure to underactuated grasps is illustrated. A more general definition is formulated, which checks the stability of the set "object + hand". Using this new definition, a simple rule is proposed for designing a hand capable of achieving 1st order form-closed grasps.

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1 Introduction

The concept of underactuation makes it possible to create grippers which automatically adapt to the geometry of the grasped object, without requiring a large number of sensors or actuators, nor a complex control strategy. Thus, using a simple binary control, such as the one usually used to drive the closing/opening motion of a parallel-jaw gripper, an underactuated gripper permits to increase the number of contact points, resulting in an enveloping grasp that should be, a-priori, more robust than a two-contact grasp. However, underactuated grippers are rarely used in the industry, first because most of gripping operations can be achieved using simple grippers dedicated to unique objects, but also because, in certain cases, underactuated grippers exhibit aberrant behavior which leads to an unstable grasp.

In Laliberté et al. (2002), a characteristic phenomenon of underactuated hands, the ejection phenomenon, is described. In certain configurations of the finger, the distribution of contact forces degenerates, i.e. some phalanxes must exert a negative force on the object in order to guarantee static equilibrium of the finger. Since a contact action is unidirectional, equilibrium cannot be attained and the ejection of the object from the hand is initiated. The ejection phenomenon highlights the need for a more in-depth investigation of the stability of a grasp exerted by an underactuated hand, considering the particular kinematics of this type of mechanism. Indeed, there has been little work dedicated to studying the stability of a grasp exerted by an underactuated hand. There exist then only few tools for designing such an underactuated hand in order to maximize its ability to stabilize an object. As a result, their design often results from an intuitive approach.

There are two main criteria which can be used to characterize the robustness of a grasp: *form-closure* and *force-closure*. These two properties permit to perform a local and static study of the stability of a grasp. Form-closure describes the capability of a hand to prevent any motion of a grasped object. Force-closure describes the capability of a hand to counterbalance any external disturbances exerted on a grasped object, by applying a combination of contact forces which respect the capabilities of actuators and the condition of friction (Bicchi, 1995). In contrast to force-closure, form-closure is a purely geometric property since it does not depend on actuators capability nor on the eventual presence of frictional forces between the gripper and the object.

These two properties have been the subject of many investigations but, to the best of our knowledge, these have never been extended to the particular case of underactuated grasps[1] (even work in Luo et al. (2004) on analysis of underactuated grasps does not deal with the particular kinematics of underactuated hands). This paper focuses on form-closure and aims to propose a simple design rule for 1st order form-closure of underactuated hands. It is based on some preliminary work introduced in Bégoc et al. (2006) and Krut et al. (2010).

2   Form-closure

2.1   Original definition

Form-closure can be described as the capability of a hand, or more generally of a set of constraining contacts, to prevent motion of a grasped object. The following definition is used for form-closure, a definition which is largely accepted in the literature:

"A grasp is said to be form-close if, and only if, for every motion of the object, at least one contact constraint is violated." (Bicchi, 1995)

The term "contact constraint" relates to the fact that the relative motion of two solid bodies in contact is constrained by the condition of non-interpenetration. This contact constraint is generally approximated to 1st order for sake of simplicity. In the major part of the literature, the configuration of the hand is assumed to be fixed, which permits to avoid the kinematic study of the hand. This assumption implies that the control position of each contact phalanx is infinitely rigid and that motors are oversized in comparison with any disturbances likely to be exerted on the object.

2.2   1st and 2nd order form-closure

A distinction must be made between two definitions: 1st order form-closure and 2nd order form-closure (Rimon and

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[1]As an abuse of language, a grasp realized by an underactuated mechanism is referred to as an underactuated grasp.
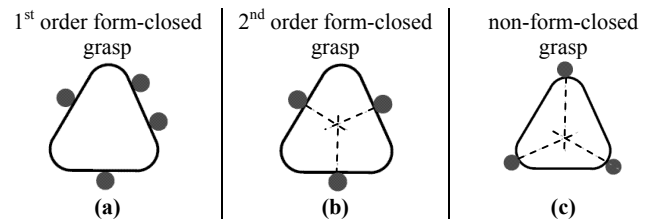

Figure 1. Illustration of grasp types (figures taken from Cheong (2006)): in situation **(a)** the object is totally immobilized, in situation **(b)** it can move with an infinitesimal rotation around the point of concurrency of the contact normals, in situation **(c)** the object is free to rotate around that point. This phenomenon can be modeled considering the local curvatures of the contact surfaces as explained in Van der Stappen et al. (2000).

Burdick, 1996). This is illustrated using the three grasps depicted in Fig. 1, where the object to be grasped remains the same but where the locations of contact points differ. In all three situations, contact points prevent the object from translating. However, if they also prevent it from rotating in case (a), they do not in cases (b) and (c): the object is free to rotate around the point of concurrency of the contact normals. After an infinitesimal rotation, the object is stopped from rotating in case (b), whereas it is free to escape in case (c). This phenomenon can be modeled considering the local curvatures of the contact surfaces as explained in Carrozza et al. (2005). Grasp (a) is 1st order form-closed, because a 1st order modeling of the grasp is sufficient to demonstrate form-closure, whereas grasp (b) is 2nd order form-closed, because 2nd order modeling is required for demonstrating form-closure.

3   Underactuation

3.1   Definition

"A mechanism is said to be underactuated, when it has fewer actuators than degrees of freedom."
(Birglen et al., 2008)

An actuator is a sub-assembly which causes relative motion between the parts to which it is attached in response to a signal (IFToMM, 2010). The number of degrees of freedom of a system is defined by the number of independent generalized coordinates required to define completely the configuration of a system at any instant of time (IFToMM, 2010). Hence, determining the number of degrees of freedom (dof) of a hand requires considering the coupling that is often introduced between the rotations of interphalanx joints. This is the case for several bionic hands, such as the DLR hands (Butterfass et al., 2001), the Robonaut's hand (Ambrose et al., 2000), the NAIST hand (Ueda et al., 2005) and the hand of humanoid robot HRP-3 (Kaneko et al., 2007).

The Grübler-Kutzbach equation cannot be applied starightforwadly to determine the degree of freedom of an underactuated hand (Krut, 2005). In fact, this method involves determining the order of a system of kinematic linear equations and it is therefore not applicable to underactuated hands which:

– use unidirectional mechanisms (non-backdrivable mechanisms or anti-return mechanisms) in the transmission of the opening/closing motion of the fingers, because these are modeled using inequalities. This is the case for many underactuated hands such as the Barrett Hand (Townsend, 2000) and the SARAH Hand (Lopez, 2001),

– use compliant bodies to transfer the motor's torque to the fingers as is the case of the RTR II hand (Massa et al., 2002), because the classical system of kinematic equations does not hold anymore.

3.2 Classification of underactuated hands

There is a large diversity of mechanical devices which enable a hand to adapt to the geometry of an object. In this paper, we propose to classify underactuated hands based on the expression of contact forces as a function of the torques exerted by the actuators on the mechanism. Hence, an underactuated hand can be:

1. differential,

2. compliant,

3. self-locking,

4. or have a combination of these three properties.

3.2.1 Differential underactuation

The first category can be characterized by the formulation given in Krut (2005). A mechanism is said to be differential when its behavior, from a kinetostatic point of view, can be described by the following equations:

$$F_{\mathrm{a}} = F_1^{\mathrm{a}} r_1 = \cdots = F_n^{\mathrm{a}} r_n \qquad (1)$$

$$\theta_a + \sum_{i=1}^{n} \frac{\theta_i^{\mathrm{a}}}{r_i^{\mathrm{a}}} = 0 \qquad (2)$$

where F_{a} is the force, or the actuation torque, exerted on the input of the differential mechanism and F_i^{a} is the force or torque transmitted to the output i. $\left(\theta_{\mathrm{a}}, \theta_1^{\mathrm{a}}, \cdots, \theta_n^{\mathrm{a}}\right)$ describes the configuration of the differential mechanism, $\left(\theta_{\mathrm{a}}, \theta_1^{\mathrm{a}}, \cdots, \theta_n^{\mathrm{a}}\right)$ the joint velocities and $\left(r_1^{\mathrm{a}}, \cdots, r_n^{\mathrm{a}}\right)$ the transmission ratios. A review of the state of the art of differential mechanisms used in underactuated grippers can be found in Birglen and Gosselin (2006).

3.2.2 Compliant underactuation

A mechanism is said to be compliant when the forces exerted on its output can be written as a function of the configuration of the mechanism and the stiffness of the mechanical elements introduced into the transmission of the closing motion of the hand:

$$\left[\begin{array}{cccc} F_{\mathrm{a}} & F_1^{\mathrm{a}} & \cdots & F_n^{\mathrm{a}} \end{array} \right]^T = \boldsymbol{R} \left[\begin{array}{cccc} \theta_{\mathrm{a}} & \theta_1^{\mathrm{a}} & \cdots & \theta_n^{\mathrm{a}} \end{array} \right]^T \qquad (3)$$

where $\boldsymbol{R}$ is the stiffness matrix of the mechanism.

3.2.3 Self-locking underactuation

The category of self-locking underactuated mechanisms is introduced in order to characterize hands which have unidirectional mechanisms in the transmission of the fingers' closing motion. Indeed, this has a strong influence on the expression of contact forces and, as a consequence, on the characteristics of the grasp since this type of mechanisms prevents all return motion of the fingers or phalanxes whatever the disturbances exerted on the grasped object. Theoretically, the contact forces could then be infinite. We define a mechanism to be self-lockable, when the configuration of the mechanism is constrained by a set of inequalities of the type:

$$\delta_i \theta_i^{\mathrm{a}} \geq 0, \ \forall i = \{1, \cdots, n\} \qquad (4)$$

$\delta_i = \pm 1$ depending on the case.

3.3 Classification of unidirectional mechanisms

The unidirectional mechanisms, on which the self-locking hands are based, provide unidirectional transmission of motion, which can be modeled by:

$$\theta_{\mathrm{out}} \geq 0 \qquad (5)$$

where θ_{out} represents the output velocity of the mechanisms. Unidirectional mechanisms can be spited in two main categories: (1) anti-return mechanisms and (2) non-backdrivable mechanisms.

3.3.1 Anti-return mechanisms

Among the available anti-return mechanisms are:

– blocking mechanisms by obstacle, such as the "pawl and ratchet" mechanism or the sliding gear,

– locking mechanisms by bracing or wedging such as a freewheel (with ramp or cam), wrap spring couplings or sliding/bracing mechanisms, such as those used in the underactuated hand designed by Lopez (2001),

– a non-return valve when fluid energy is used.

In the case of the free-wheel mechanism and wrap spring coupling, the unilateral condition is described differently:

$$\theta_{out} \geq \theta_{in} \qquad (6)$$

where θ_{out} and θ_{in} are the output and input velocities of the mechanism respectively. This condition is identical to condition (5) when the input velocity is zero.

3.3.2 Non-backdrivable mechanisms

Non-backdrivable mechanisms provide also the same unilateral condition (5). A mechanism is said to be non-backdrivable when it is incapable of transmitting motion and power from the output to the input (IFToMM, 2010), as for instance:

- the "triangular wedge" mechanism,

- The "wheel and worm drive" mechanism,

- The "rack and worm drive" mechanism,

- The "lead screw and nut" mechanism.

A non-backdrivable mechanism operates differently from an anti-return mechanism. Nevertheless, it is possible to impose a unidirectional transmission of motion $\theta_{out} \geq 0$ by maintaining a positive or null force on the input of the non-backdrivable mechanism.

In practice, it is noticeable that designers of underactuated hands prefer to introduce non-backdrivable mechanisms. The advantage of these mechanisms is that it is sufficient to invert the direction of rotation at the input in order to invert the sense of rotation at the output, and hence to enable opening of the gripper. In the case of a unidirectional mechanism, a mechanism is required to deactivate the anti-return function, as for instance the solution proposed in Lopez (2001) to deactivate a sliding/bracing mechanism.

4 Extension of form-closure to underactuated hands

The definition of form-closure, as it is usually encountered in the literature, is based on the assumption that contact points are fixed in space. When considering a robotic hand, this assumption implies to consider that the position control of each phalanx is infinitely rigid, so that the configuration of the hand remains unchanged whatever the amplitude of disturbances exerted on the object. This greatly simplifies the study of the grasp, by avoiding the kinematic study of the hand. This assumption is justified for the majority of robotic hands, for which the position of each phalanx can be independently controlled. In contrast, it is not possible to independently control the position of each phalanx when using an underactuated hand. The assumption of fixed contact points is then false.

In Krut et al. (2010), the definition of form-closure was reformulated so that it applies to the case of underactuated
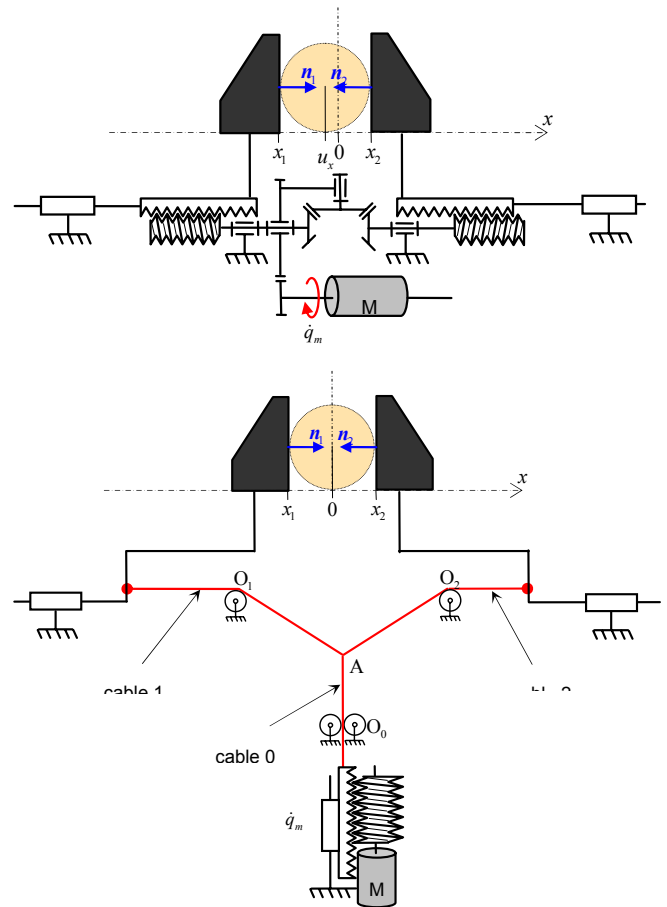

Figure 2. Diagram representing a two contact grasp.

grasps. Since immobility of contact points is not guaranteed, not only the motions of the object have to be studied but also the motions of the grasp, i.e. the motions of the overall system including the object and the hand. Thus, checking form-closure of an underactuated grasp now requires verifying that any variation in the configuration of the grasp is prevented by a set of unilateral kinematic constraints, i.e. the contact constraints and the constraints imposed by the non-backdrivable mechanisms. The definition of form-closure was reformulated as follows:

"A grasp is said to be form-closed if, and only if, for any variation of the configuration of the grasp at least one of the unilateral kinematic constraints is violated."

To illustrate this definition, two simple cases of two-finger grasps are considered (see Fig. 2). These grasps differ in terms of type of transmission used to produce the closing motion of fingers. In order to simplify this analysis, in a way that will make it intuitive, an operational space of dimension one only is considered, i.e. only the translation of the object along x is studied.

4.1 Mechanism A

The first mechanism is underactuated by a geared differential mechanism (Fig. 2a). The closing motion of each jaw is transmitted via a "wheel and worm drive" non-backdrivable mechanism. Once the two jaws are in contact, they cannot move back, meaning that the object is completely immobilized. The grasp is form-closed.

4.2 Mechanism B

The second mechanism is underactuated by a "pulley/tendon" differential mechanism. A single actuator drives the closing motion of the gripper by tightening cable 0. This tension is transmitted to cables 1 and 2 which are connected to cable 0 at point A (Fig. 2b). This device tends to move the grasped object in the centered position during the closing motion when cable 0 is tightened. Once centered, the object is immobilized. However, contrarily to the grasp exerted by mechanism (a), infinitesimal motions can still occur in this centered configuration. The grasp is 2nd order form-closed. To make it 1st order form close, extra non-backdrivable mechanisms should be added in the transmission of the closing motion of the hand. This aspect will be emphasize in next section while introducing simple design rules to achieve 1st order form-closure.

5 Design rules for 1st order form-closure of underactuated hands

5.1 The minimum number of unilateral constraints

As illustrated by these two examples, the introduction of non-backdrivable mechanisms into the transmission of the closing motion of an underactuated gripper has a direct influence on the stability of the grasp.

In this paper, mathematical formulations that could justify the above assertions are not given (see Krut et al. (2010) to get them). These assertions are based on intuition, and should help us to understand that there is an analogy between the underactuated grasps illustrated in Fig. 2 and the classical grasps illustrated in Fig. 1:

– grasps shown on Fig. 1a and Fig. 2a are both 1st order form-closed, whereas

– grasps shown on Fig. 1b and Fig. 2b are both 2nd order form closed.

This analogy allows understanding how it is possible to extend an important result from classical grasps (exerted by fully actuated grippers) to underactuated grasps: that of the minimum number of contact points necessary for 1st order form-closure. These works were initiated by Reulaux (1976) and Somov (1900), and later demonstrated by Lakshminarayana (1978), Markenscoff et al. (1990) and Reulaux

(1976). They demonstrate that $d+1$ contacts are necessary to achieve 1st order form-closure of classical grasps:

$$n_c \geq d+1 \tag{7}$$

where n_c is the number of unilateral contact constraints and d is the dimension of the configuration space of the object (3 for the planar examples depicted in Fig. 1, 6 in the general case).

By analogy, the following inequality can be written for underactuated grasps:

$$n_k \geq g+1 \tag{8}$$

where n_k is the number of unilateral constraints of the problem and g is the dimension of the grasp configuration space.

This can be stated the following way:

"At least g+1 unilateral constraints are necessary for 1st order form-closure."

The unilateral constraints of the problem are composed (see Krut et al. (2010) for more details) of the unilateral contact constraints and the unilateral constraints imposed by the unidirectional mechanisms (such as worm gears or free wheels). Hence:

$$n_k = n_u + n_c \tag{9}$$

with n_u the number of unilateral constraints imposed by the unidirectional mechanisms, and n_c is the number of unilateral contact constraints.

Additionally, the grasp configuration space is made of the configuration space of the object and the hand considered separately. Hence:

$$g = n_p + d \tag{10}$$

with n_p the dimension of the hand configuration space, that is, the number of degrees of freedom of the hand, and d is the dimension of the configuration space of the object.

5.2 The minimum number of unidirectional mechanisms

Relation (8) can be rewritten as:

$$n_u + n_c \geq n_p + d + 1 \tag{11}$$

Considering a hand with as many DOF as phalanxes, and a grasp where each phalanx exerts one contact point with the object including the palm, leads to:

$$n_c = n_p + 1 \tag{12}$$

Equations (11) and (12) enable a simple rule for designing underactuated hands, capable of performing 1st order form-closed grasps:

Table 1. Characteristics of underactuated robotic hands. The symbol – indicates that there is no underactuation or no non-backdriveable mechanisms depending on the column.

Name	No. of DOF	No. of act. for closure	No. of act. for config.	Type of underact. between fingers	Type of underact. between phalanxes	Non-backdriveable mechanisms	Reference
Soft Gripper	18	2	0	differential pulleys/cables	differential pulleys/cables	–	Hirose and Umetani (1978)
Hand of the LMS	9	1	0	differential with cables	differential pulleys/cables	–	Champeau (1991)
TU Delft Hand	5	1	0	differential with cables	differential pulleys/cables	–	De Visser and Herder (2000)
Barrett Hand	7	3	1	–	self-locking	6 wheels and worm drives	Townsend (2000)
TBM Prosthesis	15	1	0	compliant	differential four-bar	–	Dechev et al. (2001)
Southampton Hand Prosthesis	15	4	2	–	differential four-bar	6 wheels and worm drives	Light and Chappell (2000)
Lopez Hand	9	1	0	self-locking	differential pulleys/cable	9 bracing devices	Lopez (2001)
MARS	12	3	3	–	differential four-bar	–	Laliberté et al. (2002)
SARAH	10	1	1	self-locking	differential four-bar	3 wheels and worm drives	Laliberté et al. (2002)
Laval Univ. Pneumatic Hand	10	3	1	–	differential four-bar	3 motorised anti-return valves	Laliberté and Gosselin (2003)
RTR II	9	1	1	compliant	differential pulleys/cables	1 wheel and worm drive	Massa et al. (2002)
SPRING Hand	8	1	0	compliant	differential pulleys/cables	1 wheel and worm drive	Carrozza et al. (2004)
RTR IV	14	1	0	compliant	differential with cables	–	Carrozza et al. (2005)
Nasser Prosthesis	15	1	0	self-locking	differential four-bar	4 wheels and worm drives	Nasser et al. (2006)
Cyberhand	16	5	1	–	differential pulleys/cables	–	Cipriani et al. (2006)
Laval Univ. Prosthesis	17	1	0	differential pulleys/cables	differential pulleys/cables	–	Birglen and Gosselin (2006)
SDM Hand	8	1	0	differential pulleys/cables	differential with cables	–	Dollar and Howe (2007)
iLimb	11	5	1	–	differential with tendons	5 wheels and worm drives	Gow (2007)
Southampton End Effector Hand	8	1	0	differential four-bar	differential four-bar	–	Crowder (1991)

"When considering that each phalanx exerts one contact point with the object including the palm, at least d unidirectional mechanisms are required for an underactuated hand to be capable of performing 1st order form-closed grasps."

The TWIX hand, proposed by the authors, was designed according to this simple design rule (Bégoc et al., 2007). Note that for the grasps illustrated in Fig. 2, as there is no palm and as the dimension of the configuration space is $d = 1$, at least 2 unidirectional mechanisms are required for an underactuated hand to perform 1st order form-closed grasps. This witnesses why the grasp illustrated in Fig. 2a., performed by an underactuated hand having 2 unidirectional mechanisms, is 1st order form closed, while the one of Fig. 2b., performed by an underactuated hand having only one unidirectional mechanism (the actuator), is only 2nd order form-closed.

5.3 Discussion and analysis of some underactuated hands

Table 1 lists the main characteristics of various existing underactuated hands. For each hand, the table lists the number of dof, the number of actuators used to drive the closing/opening motion of the hand and the number of actuators used to modify the configuration of the hand. The type of underactuation used for the finger inputs and the phalanx inputs is listed separately, often being of different types. Finally, the number and type of the non-backdrivable mechanisms introduced in the mechanical transmission of the closing motion of the hand are indicated.

One of the major limitations of underactuated hands lies in the ejection phenomenon described in Laliberté et al. (2002). As already mentioned, in certain configurations of the finger, the force exerted by certain phalanxes on the object must be

negative to achieve static equilibrium of the finger. Because the contact forces are unilateral, this equilibrium cannot be attained, which causes a backward motion of the corresponding phalanxes. Introducing a unidirectional mechanism in the transmission of the closing motion of each phalanx prevents any backward motion of the phalanx and consequently eliminates the ejection phenomenon. This explains why a large number of underactuated hands described in Table 1 use non-backdrivable mechanisms without, however, justifying it.

On the basis of the design rule introduced in the previous section, let us review the existing underactuated hands listed in Table 1 It can be noted that, out of the 19 hands, only 3 integrate at least six unidirectional mechanisms: the Lopez hand, the Southampton hand, and the Barrett hand. The other hands in the table cannot achieve 1st order form-closed grasps. Of course they are capable of performing stable grasps, but exhibiting other types of stability such as higher order form-closure or force-closure.

Following this simple rule, when designing underactuated hands, may improve the quality of the grasp in some circumstances. For us, the best proof is that the Barrett hand, that satisfies this simple rule, is the only one that encountered success in industry. However the systematic adoption of that design rule can lead to an increased complexity of the overall mechanical structure of the hand, thus compromising the main appeal of underactuation, that is, simplicity, low cost and so on.

6 Conclusions

In this paper, the inadequation of the definition of form-closure, as largely accepted in the literature, with the case of underactuated grasps has been pointed out. The definition is based on the assumption that contact points are fixed in space; this hypothesis is no longer true when the grasp is ex-

erted by an underactuated hand. Therefore, a more general definition has been introduced, which consists in verifying that the system formed by the hand and the object is immobilized by a set of kinematic constraints. Among these constraints are the contact constraints to which the constraints imposed by unidirectional mechanisms have been added. Indeed, it has been shown, using several simple examples, that unilateral mechanisms have a relevant influence on the stability of the grasp. Hence, a new classification of underactuated hands has been proposed, based on the study of the expression of contact forces. Numerous existing underactuated hands use unilateral mechanisms, without justifying it.

Finally, this study allowed us to state a simple design rule on the minimum number of unidirectional mechanisms to be introduced into the transmission of the closing motion of the fingers of an underactuated hand, so that it is capable of producing 1st order form-closed grasps.

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