



A new magnetorheological elastomer torsional vibration absorber: structural design and performance test

Pu Gao^{1,2}, Hui Liu^{2,3}, Changle Xiang^{2,3}, Pengfei Yan³, and Taha Mahmoud³

¹School of Mechatronical Engineering, Beijing Institute of Technology, Beijing, 100081, China ²Beijing Institute of Technology Chongqing Innovation Center, Chongqing, 401120, China ³School of Mechanical Engineering, Beijing Institute of Technology, Beijing, 100081, China

Correspondence: Hui Liu (liu_hui_bit@126.com)

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Abstract. The semi-active torsional vibration absorber can effectively reduce the torsional vibration of the power-train system. In this paper, a new type of variable stiffness torsional vibration absorber with a magnetorheological elastomer (MRE) as an intelligent controlling element is designed, and the modal analysis, frequencytracking scheme, and damping effects have been studied. A transient dynamic simulation is utilized to validate the rationality of the mechanical structure, the magnetic field parameters of the absorber are matched, and the magnetic circuit simulation analysis and the magnetic field supply analysis are carried out to verify the closed magnetic circuit. The principle prototype of the innovative vibration absorber is manufactured, the magnetic field strength of the absorber is tested by a Gauss meter, and the results show the efficacy of magnetizing the vibration absorber with a conductive slip ring by solving the magnetizing problem of the rotating parts of the vibration absorber. A special-purpose test rig with a torsional vibration exciter as a power source has been implemented. A comparative experiment has been carried out to test the frequency shift characteristics and authenticate the vibration-reduction effect of the new MRE torsional vibration absorber.

1 Introduction

The vibration of the power-train system is one of the essential sources of vehicle vibration. It usually consists of an engine, clutch, gearbox, drive shaft, differential, wheel, and many other components, which is a wide-band vibration system and has multiple natural vibration frequencies (Couderc et al., 1998; Liu, 2003). External excitations result in a much more complex signal with various frequencies and amplitudes (Zhang et al., 2003; Crowther, 2004). The aforementioned factors may cause the system to traverse different resonance zones in a wide frequency range, thus leading to vibration deterioration, seriously affecting the performance and reliability of the vehicle significantly along with distressing the passengers. Consequently, it is vital to study the torsional vibration reduction of the vehicle power train.

The torsional vibration problem of the power-train system can be settled by the following three methods.

- 1. New materials, new structures, and new technology can be utilized to enhance the overall dynamic characteristics of the system (Shangguan et al., 2016; Londhe and Yadav, 2008; Nagar et al., 2013).
- 2. Advanced analysis methods can be applied to optimize the power-train system component structures: for instance, the dynamic modification of gears is used to improve the gear-meshing state of the gearbox, differential, and main reducer (Parag and Ahmet, 2002; Li et al., 2007; Liu et al., 2016).
- 3. The clutch disk torsional damper (Chen, 2005), Geislinger coupling (Xiang and Geng, 2004), dual-mass flywheel torsional damper (Song et al., 2012; Shi et al., 2009), and positive–negative stiffness parallel torsional damper can be mounted on the power transmission path to reduce the fluctuation torque of the system (Liu et al., 2018).

Based on the comprehensive analysis of the abovementioned vibration-reduction methods, the torsional vibration damper approach is considered the most efficient method. The passive torsional vibration damper has a simpler structure and lower cost than the active torsional vibration damper. However, the passive-type vibration reduction is limited. The existing semi-active and active vibration dampers can overcome this disadvantage. Nevertheless, active and semi-active vibration dampers are complex and very expensive, and hence their popularization and application are hindered. Therefore, it is crucial to design a new semi-active torsional damper with a simple structure and excellent damping performance. In this research, an adaptive tuned torsional vibration absorber is designed with the magnetorheological elastomer as an intelligent control element to reduce the torsional vibration of the power-train system.

The vibration absorber consists of a dynamic mass (inertia term), an elastic element (spring term), and a damping element (damping term), which can produce vibrationabsorption forces to neutralize the vibration of the main system. When the natural frequency of the vibration absorber is equivalent to the excitation frequency, it can effectively reduce the system vibration. In recent years, researchers have sought to study magnetorheological elastomer (MRE) absorbers, and great achievements have been contributed in such fields. Nguyen et al. (2020) proposed a novel MREbased absorber, and an adaptive neural network controller was designed. The Dong et al. (2020) MRE variable stiffness torsional vibration absorber was designed to alleviate the vibration of a power-train system. Ginder et al. (2001) studied the variable stiffness characteristics of the MRE and then designed a new type of MRE dynamic vibration absorber; moreover, the frequency shift range reached 100 Hz. In Albanese and Cunefare (2003a, b), a compression-mode MRE vibration absorber based on the controllable compression stiffness characteristics of the MRE was devised, the frequency shift characteristics were tested, and the control method by the experiments was investigated. Ni et al. (2009) and Deng and Gong (2007) designed a shearmode MRE dynamic vibration absorber; after that its frequency shift characteristics were tested by experiments. His research team also proposed a shear-compression hybridmode MRE vibration absorber, and the numerical simulation is carried out to authenticate the consistency of the designed structure. Lerner and Cunefare (2008) studied the frequency shift performance of the MRE vibration absorber in various shear and compression working modes. The Yu et al. (2007) and Shi et al. (2016) magnetorheological elastomer was prepared independently, the properties of the material were assessed, variable stiffness mechanisms were investigated, and, furthermore, a semi-active vibration absorber with virtuous vibration-reduction performance was proposed. Hoang (2011) and Hoang et al. (2009) designed a semi-active MRE torsional vibration absorber for the vehicle power train, and the frequency shift characteristics using the hammer test were evaluated. Xin et al. (2017) and Qian et al. (2017) designed a vertical direction MRE vibration absorber for the vehicle mounting system, yet he studied its vibration-absorption performance; moreover, its control strategy was perfected. Rao et al. (2014) designed a shearmode MRE dynamic vibration absorber to reduce the longitudinal vibration of the power-train system. Based on the indepth study of the torsional vibration characteristics of the vehicle power-train system, Gao et al. (2019a, b) proposed the concept of a new MRE torsional vibration absorber to reduce the torsional vibration of the power-train system.

So many achievements have been made in the adaptive tuned vibration absorber field. Nonetheless, technical issues still exist, such as the following.

- 1. Due to the rotation of the MRE torsional vibration absorber, in the structural design of the new type vibration absorbers, the magnetic supply of the electromagnetic coil which controls the MRE variable stiffness is a technical challenge.
- 2. The frequency shift characteristics of the MRE torsional vibration absorbers are vibration-reduction cornerstones for the main vibration system. Almost all of the preceding test rigs of the frequency shift characteristics are for vertical direction vibration absorbers. As a result, it is necessary to build a special-purpose test rig for the frequency shift characteristics of the torsional direction vibration absorbers.

The main objective of this work is to tackle these above issues; a summary of this research is as follows. In Sect. 2, the principle of torsional vibration absorption is briefly introduced. In Sect. 3, the basic structure of a new type of MRE torsional vibration absorber is designed, the transient dynamic simulation is carried out to validate its rationality, the magnetic field parameter is matched and then the magnetic circuit simulation analysis is carried out, the prototype of the vibration absorber is manufactured, and the magnetic field supply test is carried out. In Sect. 4, a special vibration test rig is built to estimate the frequency shift characteristics of the innovative torsional vibration absorber, and the comparative experiments corroborate the effect of the new vibration absorber; Sect. 5 is the conclusions and highlights of this paper.

2 Torsional vibration-absorption principle

2.1 Dynamic model of the torsional vibration absorber

The dynamic model of the torsional vibration absorber has been derived, as shown in Fig. 1; the dynamic model is composed of the main system and torsional vibration absorber.



Figure 1. Dynamic model of the torsional vibration absorber.

Table 1. Natural frequencies and corresponding damping ratios.

Order	Natural frequency (Hz)	Damping ratio (%)
1	8.19	0.01
2	53.49	0.06

According to Fig. 1, the dynamic equations of the torsional vibration system can be obtained:

$$J_{1}\ddot{\theta}_{1}(t) + k_{1}\theta_{1}(t) + c_{1}\dot{\theta}_{1}(t)$$
(1)
+ $k_{2}[\theta_{1}(t) - \theta_{2}(t)] + c_{2}[\dot{\theta}_{1}(t) - \dot{\theta}_{2}(t)] = f(t),$
 $J_{2}\ddot{\theta}_{2}(t) + k_{2}[(\theta_{2}(t) - \theta_{1}(t))] + c_{2}[\dot{\theta}_{2}(t) - \dot{\theta}_{1}(t)] = 0,$ (2)

where J_1 and J_2 are the inertia of the main system and the dynamic inertia of the torsional vibration absorber, respectively; θ_1 and θ_2 are the torsional angular displacements of the main system and the torsional vibration absorber, respectively; k_1 and k_2 are the torsional stiffness of the main system and the torsional vibration absorber, respectively; c_1 and c_2 are the torsional damping of the main system and the torsional vibration absorber, respectively; f(t) is the external excitation torque, and ω is the frequency of the external excitation.

2.2 Modal analysis

Assume that the torsional stiffness of the torsional vibration absorber k_2 is fixed, $15000 \text{ Nm rad}^{-1}$; the torsional vibration absorber is passive, while the torsional stiffness of the main system k_2 is $18000 \text{ Nm rad}^{-1}$; J_1 and J_2 are 3.0 and 0.3 kg m², respectively; c_1 and c_2 are 2.0 and $10.0 \text{ Nm s rad}^{-1}$, respectively; The natural frequencies and corresponding damping ratios of the system can be obtained, as shown in Table 1.

The modal shapes of each natural frequency of the system are shown in Fig. 2.

Table 1 and Fig. 2 show that the torsional vibration absorber has a considerable influence on the natural vibration characteristics of the main system, and the modal analysis of the torsional vibration absorber lays a worthy foundation for the new MRE torsional vibration absorber.



Figure 2. Modal shapes of each natural frequency.

2.3 Frequency-tracking scheme of the variable stiffness torsional vibration absorber

Presume that the torsional stiffness of the torsional vibration absorber k_2 is variable: then the torsional vibration absorber is a semi-active absorber, and hence the frequency-tracking scheme of the semi-active absorber can be obtained from the following equations.

The Fourier transform is applied to Eqs. (1) and (2):

$$-\omega^{2}J_{1}\Theta_{1}(\omega) + k_{1}\Theta_{1}(\omega) + j\omega c_{1}\Theta_{1}(\omega)$$
(3)
+ $k_{2}[\Theta_{1}(\omega) - \Theta_{2}(\omega)] + j\omega c_{2}[\Theta_{1}(\omega) - \Theta_{2}(\omega)] = F(\omega),$
- $\omega^{2}J_{2}\Theta_{2}(\omega) + k_{2}[\Theta_{2}(\omega) - \Theta_{1}(\omega)]$ (4)
+ $j\omega c_{2}[\Theta_{2}(\omega) - \Theta_{1}(\omega)] = 0,$

where $F(\omega)$, $\Theta_1(\omega)$, and $\Theta_2(\omega)$ are the Fourier transform expressions of f(t), $\theta_1(t)$, and $\theta_2(t)$, respectively.

Solving the above equations, the torsional angular displacements of the main system and the torsional vibration absorber are acquired:

$$\Theta_1(\omega) = \frac{\left(-J_2\omega^2 + j\omega c_2 + k_2\right)\Theta_2(\omega)}{j\omega c_2 + k_2},\tag{5}$$

$$\Theta_2(\omega) = \frac{F}{-J_1\omega^2 + j\omega c_1 + k_1}.$$
(6)

Based on Eq. (4), with the aim of reducing the vibration displacement of the main system to null, the following equation must be satisfied:

$$-J_2\omega^2 + j\omega c_2 + k_2 = 0, (7)$$

assuming that the damping of the torsional vibration absorber is neglected, that is, $c_2 = 0$. As demonstrated in Eq. (5), if the vibration displacement of the main system needed to be null, the natural frequency of the torsional vibration absorber ought to be equal to the frequency of external excitation torque, $\omega_2 = \sqrt{k_2/J_2} = \omega$. Therefore, $k_2 = J_2\omega^2$ is usually



Figure 3. Dynamic amplification factors with different absorber damping factors.

used as the frequency-tracking scheme of the semi-active absorber, which is also considered to be the basis of the control strategy of the semi-active torsional vibration absorber in engineering applications.

2.4 Damping effect of semi-active absorber

Assuming the static angular displacement of the main system is $A_0 = F/k_1$, the ratio of the dynamic inertia of the vibration absorber to the inertia of the main system is $\mu = J_2/J_1$. The natural frequency ratio of the vibration absorber to the main system is derived as $b = \omega_2/\omega_1$. The ratio of the external excitation frequency to the natural frequency of the main system can be written as $r = \omega/\omega_1$; the damping ratio of the vibration absorber is represented as $\zeta = c_2/2J_2\omega_2$. The dynamic amplification factor A_1/A_0 of the main system is

$$\frac{A_1}{A_0} = \sqrt{\frac{(r^2 - b^2)^2 + (2\zeta r)^2}{\left[\mu r^2 b^2 - (r^2 - 1)(r^2 - b^2)\right]^2}}.$$
(8)

The dynamic amplification factor can represent the vibrationreduction effect of the vibration absorber. The parameters of the semi-active absorber can be set as $\mu = 0.25$, b = 1, and r = 1. The dynamic amplification factors with different absorber damping factors are shown in Fig. 3.

From Fig. 3, it can be observed that when the absorber damping factor increases from 0.01 to 0.20, the damping factors have an insignificant effect on the vibration-reduction performance of the frequency adaptive tuned vibration absorber.

3 Structural design of torsional vibration absorber

3.1 Mechanical structure design

An innovative MRE variable stiffness torsional vibration absorber is designed, as shown in Fig. 4. The new torsional vibration absorber is installed in a proper position of the power transmission path in the form of a coupling. It rotates with



1- upper yoke 2- electromagnetic coil 3-iron core 4- MRE 5- lower yoke 6- magnetic resistance plate 7- connecting disc 8- circular plate

Figure 4. Basic structure of the MRE vibration absorber.

the transmission shaft, and the outer contour of the vibration absorber is a rotationally symmetric ring. The absorber is mainly composed of four fan-shaped magnetorheological vibration-absorbing structures. The fan-shaped vibrationabsorbing structure consists of an upper yoke (1), two electromagnetic coils (2), two iron cores (3), two MREs (4), and a lower yoke (5), forming a closed magnetic circuit. The electromagnetic coil (2) is installed on the upper yoke and connected with the external controller through the conductive slip ring. The circular plate (6) is used to connect the four fan-shaped structures into a ring to make them equivalent to the dynamic inertia from the perspective of the dynamics. A magnetic resistance plate (6) is equipped between the lower yoke (5) and the connecting disc (5), so that the fan-shaped structure is an independent closed magnetic field from the perspective of the magnetics.

The fan-shaped MRE structure has three advantages.

- 1. Four fan-shaped MRE structures are evenly installed in the main vibration system, which is connected by the circular plate, forming equivalent dynamic inertia with rotary symmetry. This design can efficiently eliminate the centrifugal force and is more efficacious in reducing torsional vibrations.
- 2. The fan-shaped MRE structure includes double electromagnetic coils, and the MREs are installed on the main magnetic flux path, which can acquire a larger magnetic field with less power consumption.
- 3. The variable shear stiffness of the MRE can be transformed into the equivalent variable torsional stiffness of the absorber by this fan-shaped structure.

The variable stiffness element of the vibration absorber is MREs (4) and works in the shear mode, as shown in Fig. 5.

As shown in Fig. 5, F is the shear direction external load; H is the vertical direction external magnetic field; A is the cross-sectional area of the MRE; and h is the thickness of the MRE. In shear working mode, the direction of the external



Figure 5. MREs working in the shear mode.

load F is perpendicular to the direction of the external magnetic field H, and the direction of the external magnetic field H is parallel to the forming chain's direction of the MRE ferromagnetic particles (Tesfahunegn et al., 2011).

The MRE is a viscoelastic solid material that has a shear complex modulus, which consists of a storage modulus and a loss modulus:

$$G = G' + iG'',\tag{9}$$

where G is the complex modulus reflecting the comprehensive shear performance, whereas G' is the storage modulus reflecting the elastic property of the viscoelastic solid which encounters perceptible alterations in the magnetic field. The alterations of the complex shear modulus with the external magnetic field are close to the storage modulus. G" shows that the loss modulus with an insignificant value results in a slight change in the magnetic field that reflects the capacity of dissipating energy. As a result, the storage modulus can characterize the magnetic-induced shear performance of the MRE (Xiang et al., 2018).

The magnetic-induced shear storage modulus of the MRE can be expressed as

$$G' = G_H = \tau/\gamma = \frac{-\frac{1}{2}\mu_0 \left(\frac{H_0}{1+\chi_{\text{eff}}}\right)^2 \frac{\partial\chi_{\text{eff}}}{\partial\gamma}}{\gamma},\tag{10}$$

where μ_0 is the permeability of the vacuum, H_0 is the external magnetic field strength, χ_{eff} is the effective magnetic susceptibility, and γ is the shear strain.

The relationship between shear modulus and shear stiffness can be obtained from

$$k_{\tau} = \frac{G_H A}{h},\tag{11}$$

where k_{τ} is the shear stiffness of the MRE, G_H is the magnetic-induced shear modulus, A is the cross-sectional area, and h represents the effective working height.

The U-CAN dynamic test apparatus is mainly used to examine the shear stiffness in the different magnetic field, as shown in Fig. 6. The diameter of the sample is 30 mm, the height is 6 mm, and the whole test speed is set to $10 \text{ mm} \text{min}^{-1}$, at room temperature. The shear stiffness of

Table 2. Shear stiffness with different external magnetic fields.

Order	Magnetic field (mT)	Shear stiffness $(N m^{-1})$
1	0	36 930
2	370	39 860
3	500	45 470

 Table 3. Equivalent torsional stiffness with different external magnetic fields.

Order	Magnetic field (mT)	Torsional stiffness $(N m^{-1})$
1	0	12 665
2	370	13 670
3	500	15 594

the MREs with different external magnetic fields can be acquired, as indicated in Table 2.

Referring to the shear working mode, the equivalent torsional stiffness of the new vibration absorber can be achieved:

$$k_{\rm A} = n R^2 k_{\tau},\tag{12}$$

where k_A is the equivalent torsional stiffness of the vibration absorber, *n* is the number of the MREs in the shear mode, n = 8, and *R* is the center distance between the shear working position of the MRE and the torsion center of the vibration absorber, as shown in Fig. 4. The equivalent torsional stiffness of the vibration absorber can be obtained, as shown in Table 3.

In addition to the components in Fig. 4, other components of the vibration absorber also include the speed and torque sensor, controller, a programmable power, and a conductive slip ring. First, the sensors are used to acquire the speed and torque signals. Then, the controller is used to identify the dominant frequency of the external excitation and compute the optimal control current. Next, the current enters the vibration absorber through the conductive slip ring from the programmable power for the purpose of controlling the magnetic field of the electromagnetic coil. Finally, the real-time control of the variable stiffness of the vibration absorber makes its natural frequency effectively follow the dominant frequency of external excitation; the detailed process is shown in Fig. 7.

When the vibration absorber starts working, the electromagnetic coil will produce a changing magnetic field to control the shear stiffness of the MRE in real time, which changes the natural frequency of the vibration absorber; let it track the external excitation dominant frequency. Leading to the resonance of the equivalent dynamic inertia of the vibration absorber results in absorbing the vibration energy of the power transmission path. Aiming for every key vibration frequency band of the power-train system, the variable stiff326



Figure 6. U-CAN dynamic test apparatus.







Figure 8. Simulation results of the vibration response.

ness torsional vibration absorber can be installed in various positions to suppress the wide frequency band vibration of the system.

3.2 Transient dynamic simulation of the MRE torsional vibration absorber

In order to be able to authenticate the consistency of the presented structural design, transient dynamic simulation is utilized to the torsional vibration absorber. The input is loaded with an external torque excitation or a swept frequency (20– 60 Hz). The simulation results without a magnetic field are presented in Fig. 8. The vibration accelerations of the outer ring and inner ring are accumulated, the fluctuating torques can be calculated, and then the signals in the time domain are transformed into the frequency domain, as shown in Fig. 9.

From Fig. 9, it can be noticed that the natural frequency of the MRE torsional vibration absorber without a magnetic field is 35.00 Hz. The above transient dynamic simulation provides an effective reference for the following performance test.

3.3 Magnetic circuit simulation and magnetic field supply analysis

3.3.1 Magnetic field parameters matching for vibration absorbers

The proposed torsional vibration absorber consists of four fan-shaped MRE vibration-absorbing structures. The threedimensional model and sectional drawing of the fan-shaped MRE vibration absorbing structure are shown in Fig. 10.

The total magnetoresistance of the fan-shaped structure can be calculated by the following formula:

$$\sum_{i=1}^{6} R_{\rm mi} = R_{\rm m1} + R_{\rm m2} + R_{\rm m3} + R_{\rm m4} + R_{\rm m5} + R_{\rm m6}, \qquad (13)$$

where R_{m1} , R_{m2} , R_{m3} , R_{m4} , R_{m5} , and R_{m6} are the magnetoresistances of the upper yoke (1), iron core (2), MRE (4), lower yoke (5), MRE (4), and iron core (2), respectively.

The magnetoresistance can be expressed as

$$R = \frac{L}{\mu S},\tag{14}$$



(a) Vibration response in the time domain

Figure 9. Vibration responses of the outer ring and inner ring.



1- upper yoke 2- iron core 3- electromagnetic coil 4- MRE 5- lower yoke

Figure 10. Fan-shaped MRE structure.

where L is the length, μ is the magnetic permeability, and S is the section area of the magnetic field.

Since the magnetic permeability of the MRE is much lower than the iron, the magnetic resistance of the magnetic circuit is mainly caused by MRE (Zhu et al., 2007), and Eq. (11) can be simplified as

$$\sum_{i=1}^{6} R_{\rm mi} \approx R_{\rm m3} + R_{\rm m5}.$$
(15)

In the series magnetic circuit, the magnetic flux across every component is equal in magnitude, and the magnetic potential of the magnetic circuit can be expressed as

$$F = \Phi \sum R_{\rm m} = NI, \tag{16}$$

where F is the magnetic potential, Φ is the magnetic flux, N is the coil turns, and I is the current of the electromagnetic coil.

Substituting the maximum flux density, magnetic permeability, and physical size of the MRE into the above equations, the coil turns can be obtained, N = 400, and the current *I* is 3 A. Based on the above-mentioned parameters, the MRE can reach its maximum magnetic flux density.

3.3.2 Magnetic circuit simulation analysis

Maxwell software is used to simulate the magnetic circuit of the fan-shaped vibration-absorption structure. Such an approach is utilized to guarantee the closed magnetic circuit



(b) Vibration response in the frequency domain

Table 4. Magnetic circuit simulation parameters.

Vacuum	MRE geometry	Coil	Current
permeability	size	turns	
$4\pi \times 10^{-7} \mathrm{Hm^{-1}}$	$\phi 30 \times 17 \mathrm{mm}$	400	3 A



Figure 11. Magnetic circuit simulation results.

and to cover the required magnetic field range of the MRE variable stiffness. The corresponding magnetic circuit simulation parameters are exhibited in Table 4.

The magnetic circuit simulation results of the fan-shaped MRE vibration-absorption structure are shown in Fig. 11.

From the simulation results in Fig. 11, it can be concluded that the fan-shaped structure can form a closed magnetic circuit, while if the current of the electromagnetic coil is 3 A, the magnetic flux density passing through the MRE can exceed 500 mT, meeting the required magnetic field range.

By taking into consideration the structural arrangement, magnetic circuit leakage, uncertainty factors, and other ambiguities, the parameters of the fan-shaped MRE vibrationabsorption structure can be decisively achieved, as indicated in Table 5.



(a) MREs

(b) Electromagnetic coil (c) Disassembly parts

(d) Front view

(e) side view

Figure 12. Principle prototype of the MRE vibration absorber.

Table 5. Magnetic field parameters of the fan-shaped structure.

Wire diameter	Current	Coil turns	Coil resistance	Core diameter	Core length
0.7 mm	3 A	515	2.4 Ω	25 mm	53 mm



Figure 13. External magnetic field supply test.

3.3.3 Principle prototype and magnetic field power supply analysis

Based on the mechanical structure design in Sect. 3.1, the principle prototype of the vibration absorber is assembled. Figure 12 shows the genuine purpose of the innovative MRE vibration absorber, Fig. 12a shows the MREs, Fig. 12b shows the electromagnetic coil, and Fig. 12c is the overall disassembly parts, Fig. 12d the overall front view, and Fig. 12e the overall side view.

The external programmable power is used to supply power to the fan-shaped structure of the vibration absorber through the conductive slip ring; the actual magnetic field test rig is shown in Fig. 13. The magnetic field near the MRE is 250-300 mT, while in the middle zone close to the magnetic circuit, the magnetic field can reach the required value of 500 mT.

The experimental data establish the rationality of the machine-designed structure of the MRE torsional vibration absorber. Nevertheless, the magnetic supply problem of the rotating electromagnetic coils is effectively solved by using the conductive slip ring.

4 **Frequency shift characteristics and** vibration-reduction performance assessment

The torsional vibration absorber utilizes the frequency shift characteristics to preclude the natural vibration frequency from the sensitive vibration frequency band which is generated from external excitations. By such a technique, the reduction of the torsional vibrations of the power-train system can be achieved. It is necessary in addition to assess the dynamic characteristics and confirm the impact of vibration reduction.

4.1 Torsional vibration exciter test rig

With the intention of evaluating the frequency shift characteristics of the new torsional vibration absorber, a torsional vibration test rig with a torsional vibration exciter operating as the power source is built, as elucidated in Fig. 14. Figure 15 is a realistic photo of the device being used.

The torsional vibration exciter is manufactured by the XCITE company. The signal acquisition system is produced by the LMS company, and the LMS.test.lab software is employed with the purpose of compiling and post-processing the vibration response signal.

In the beginning, the hydraulic pressure pump starts to make sure that the pressure of the torsional exciter reaches 3000 Psi. Then, the LMS.test.lab software is programmed as follows: the sampling frequency is 12800 Hz and the data acquisition time under sweep frequency excitation is 250 s. After that, the sweep frequency range of the torsional exciter is set to 5–80 Hz, and the vibration amplitude is 36 Nm.

4.2 Comparative experiment of vibration-reduction performance

The steel cylinders of the same geometric size as the MRE cylinder are manufactured, as shown in Fig. 16, to be embedded in the fan-shaped structure, replacing the MRE cylinders.



Figure 14. Schematic diagram of the torsional exciter test rig.



(a) Torsional exciter system and vibration absorber test prototype (b) Data acquisition system and main controller of the vibration exciter

Figure 15. Real layouts of the test rig.



Figure 16. Steel cylinders.

Then the outer ring dynamic inertia of the vibration absorber is rigidly connected to the connecting disc.

The sweep frequency excitation experiment is conducted on the test rig. At the outset, the steel and MRE cylinders are installed on the fan-shaped structure individually. Then, the vibration response signals of the input and output ends of the two structures are collected as shown in Fig. 17a and b. Later, these two signals are compared with the vibration response signals of the torsional vibration absorber with the magnetic field 500 mT, as shown in Fig. 17c.

It can be observed from Fig. 17a that the vibration response signals at the input and output terminals of the steel rigid structure are different. The vibration response amplitude decreases from the initial value of 14.93 to 11.14 Nm after passing through the steel rigid structure, where the vibration amplitude decreases by 25.39 %. In some frequency bands, the system tends to vibrate in a deterioration manner, which is due to additional inertia added to the test system. It can be noticed from Fig. 17b and c that after the vibration passes through the vibration absorber with MRE cylinders, the magnetic field is null. The vibration response amplitude decreases from 23.20 to 13.02 N m, attaining a 43.88 % reduction.

Once the magnetic field is 500 mT, the vibration response amplitude decreases from 24.78 to 12.57 Nm, achieving 49.27 % vibration amplitude reduction. Hence, it can be concluded that the vibration-reduction effect of the torsional vibration absorber with MRE cylinders can acquire a preferable vibration-reduction level than the steel rigid structure in the entire frequency range. The aforementioned outcomes authenticate the excellence of the vibration-reduction effect of the proposed MRE cylinder vibration absorber.

In order to precisely investigate the frequency shift characteristics of the proposed MRE vibration absorber, the vibration response signals at the output in the time domain of Fig. 17 are converted into the frequency domain; subsequently, the natural frequencies of the three structures can be obtained, as shown in Fig. 18.

It can be ascertained from Fig. 18 that the natural frequency of the steel rigid structure with steel cylinders is



(a) Signals at the input and output ends with steel cylinders



(b) Signals at the input and output ends with MRE cylinders, the magnetic field 0 mT



(c) Signals at the input and output ends with MRE cylinders, the magnetic field 500 mT

Figure 17. Comparison of vibration responses of different fan-shaped structures.

30.81 Hz when the external magnetic field is null, while the natural frequency of the structure with MRE cylinders is 35.32 Hz, which is consistent with the simulation result in Fig. 9. On the other hand, when the external magnetic field is 500 mT, the natural frequency of the structure with MRE cylinders is 40.09 Hz.

Compared to the steel rigid structure, the natural frequency of the MRE structure moves backward by 14.64 %; in addition, compared with the external magnetic field being null, the natural frequency of the MRE structure with a magnetic field of 500 mT moves backward by 13.51 %. These comparative results demonstrate that the frequency shift phenomenon of the proposed vibration absorber is palpable and tangible, particularly when the absorber works under a 500 mT magnetic field.

Above and beyond, it became apparent that the amplitude of the natural frequencies increases with different structures and by the magnetic field increasing, for the reason that the input excitations are dissimilar. In addition, the input excitation of the MRE structure with a magnetic field of 500 mT exceeds the other two conditions; hence, the comparison of the amplitudes is worthless. The vibration-reduction amplitudes are crucial, the three conditions are 25.39 %, 43.88 %,



Figure 18. Natural frequencies of three structures.

and 49.27 %, and the MRE structure with a magnetic field of 500 mT has a better vibration-reduction performance.

The comparison of the vibration response signals in the time domain validates the quality of the vibration-reduction performance of the proposed vibration absorber. The comparison between the vibration response signals in the frequency domain attests to the superiority of the new MRE torsional vibration absorber in the field of the frequency shift characteristics.

5 Conclusions

- 1. A new type of MRE torsional vibration absorber is devised. The modal analysis, the frequency-tracking scheme, and the damping effect are intensely studied.
- 2. A transient dynamic simulation is carried out to validate the rationality of the machine structure. The magnetic field parameters have been reasonably designed. Moreover, the magnetic circuit simulation analysis and the magnetic field supply analysis have been performed to substantiate the intellectual of the basic mechanical structure design of the innovative vibration absorber.
- 3. A special vibration test rig with a torsional vibration exciter has been built so as to assess the frequency shift characteristics of the torsional direction vibration absorber. Additionally, a comparison of the vibration-reduction amplitudes demonstrates its outstanding vibration-reduction performance.

Code and data availability. All the data and code are shown in the paper.

Author contributions. PG and HL designed the new torsional vibration absorber; PG and PY proposed the research methods; PG and HL carried out the experiments; PG, HL and CX analysed experimental results. PG, PY and TM wrote the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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